

# REQUIRED RESERVES AS A CREDIT POLICY TOOL

*(joint with Enes Sunel and Temel Taşkın)*

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New Consensus Emerging from the Crisis?

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# INTRODUCTION

# Macroprudential Policies and Financial Stability

- ▶ **Required reserves ratios** (RRR) have been used as a macroprudential policy tool in a number of emerging economies (e.g. Brazil, China, Colombia, Peru, and Turkey).
- ▶ In particular, they use reserve requirements to curb **excessive credit growth** in boom episodes and to ease **financial constraints** in bad times.
- ▶ The main aim is to reduce the **procyclicality** of financial sector.

# Motivating Questions

- ▶ How do **time-varying** macroprudential RRR policies affect
  - ▶ Real and financial cycles of an economy in response to adverse macroeconomic and financial shocks.
- ▶ Impact of alternative RRR policies on **volatilities and cyclicity** of financial system.
- ▶ **Optimal intensity** of alternative RRR policies.
- ▶ **Effectiveness** of RRR policies in **different economic structures** (ex. highly leveraged financial system).

# Building Blocks

- ▶ Quantitative monetary DSGE model with banks
  - ▶ Households face cash-in-advance (CIA) constraints.
  - ▶ Agency problem between households and banks as in G&K (2011).
  - ▶ Banks are subject to time-varying RRR that **countercyclically** responds to **expected credit growth**.
  - ▶ Simulate the economy in the face of productivity and financial shocks under two different RRR policy regimes: **time-varying and fixed**.
  - ▶ Investigate the **effectiveness** of alternative time-varying RRR policies that respond to expected asset price growth and output growth.
  - ▶ Conduct welfare analysis of alternative time-varying RRR policies compared to fixed RRR policy through loss function approach.

# Main Results

- ▶ Time-varying RRR rule **countervails** the negative effects of F.A. mechanism triggered by adverse macroeconomic and financial shocks.
- ▶ Counter-cyclical RRR rule **reduces** volatilities of key real and financial variables in response to macro shocks.
- ▶ Time-varying RRR policy reduces **the intertemporal distortions** created by the credit spread at the expense of **higher inflation volatility**.
- ▶ The **effect** of time-varying RRR policy is **bigger** in **high risk economy** where loan-deposit spread is **higher** and the leverage of the banking sector is **lower**.

## Related Literature

- ▶ Banking  $\mapsto$  Gertler and Karadi (2011), Mimir (2011).
- ▶ Required reserves  $\mapsto$  Glocker and Towbin (2011), Montoro (2011).
- ▶ Countercyclical time-varying macro-prudential policy  $\mapsto$  Angeloni and Faia (2009), Christensen et al. (2011).
- ▶ Contribution
  - ▶ Explore the role of RRR policy in response to **financial shocks**.
  - ▶ Focus on the **composition of the assets side** of the balance sheet rather than **size** of the balance sheet.
  - ▶ Impact of alternative types of RRR rules on volatilities and cyclicity of financial sector.



## THE MODEL

# Framework

## ▶ Households

### ▶ Household's Problem

- ▶ Workers supply labor,  $h_t$  and return their wage incomes,  $w_t h_t$  to H.H.
- ▶ Households face cash-in-advance (CIA) constraints.
- ▶ Each banker manages an intermediary and transfers earnings back.
- ▶ H.H. owns intermediaries that its bankers manage.

## ▶ Financial Intermediaries

### ▶ Bank's Problem

- ▶ Collect deposits,  $b_{t+1}$  from households, combine it with their own net worth,  $n_t$  and purchase firms' shares,  $q_t s_t$ .
- ▶ They are subject to financial shocks,  $\omega_t$  (shocks to bank net worth).
- ▶ Agency problem between households and banks, leading to endogenous capital constraints for banks in obtaining funds from households.
- ▶ Banks are subject to time-varying RRR,  $rr_t$ , that counter-cyclically responds to expected credit growth.

## ▶ Non-financial Firms

### ▶ Firm's Problem

- ▶ finance capital acquisition,  $K_{t+1}$  each period via issuing equities,  $s_t$  and selling them to banks at the price of capital,  $q_t$ .

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# Government

- ▶ Money supply is assumed to grow at a constant rate  $\bar{\mu}$

$$M_{0t+1} = \exp(\bar{\mu})M_{0t}$$

- ▶ Required reserves ratio follows a time-varying rule in response to deviations of **expected future credit growth**.

$$rr_t = \bar{r}r + \phi E_t \left[ \log(q_{t+1}s_{t+1}) - \log(q_t s_t) \right]$$

where  $\phi > 0 \Rightarrow$  relax financial markets when credit is shrinking

- ▶ The money market equilibrium necessitates

$$M_{0t+1} = M_{t+1} + P_t rr_t b_{t+1}$$

- ▶ Increases in the monetary base are rebated to households through lump-sum transfers

$$T_t = M_{0t+1} - M_{0t}$$

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# Shock Processes

- ▶ Productivity shocks

$$z_{t+1} = \rho_z z_t + \epsilon_{t+1}^z$$

$$\epsilon_{t+1}^z \sim N(0, \sigma_z)$$

- ▶ Financial shocks

$$\omega_{t+1} = \rho_\omega \omega_t + \epsilon_{t+1}^\omega$$

$$\epsilon_{t+1}^\omega \sim N(0, \sigma_\omega)$$

# QUANTITATIVE ANALYSIS

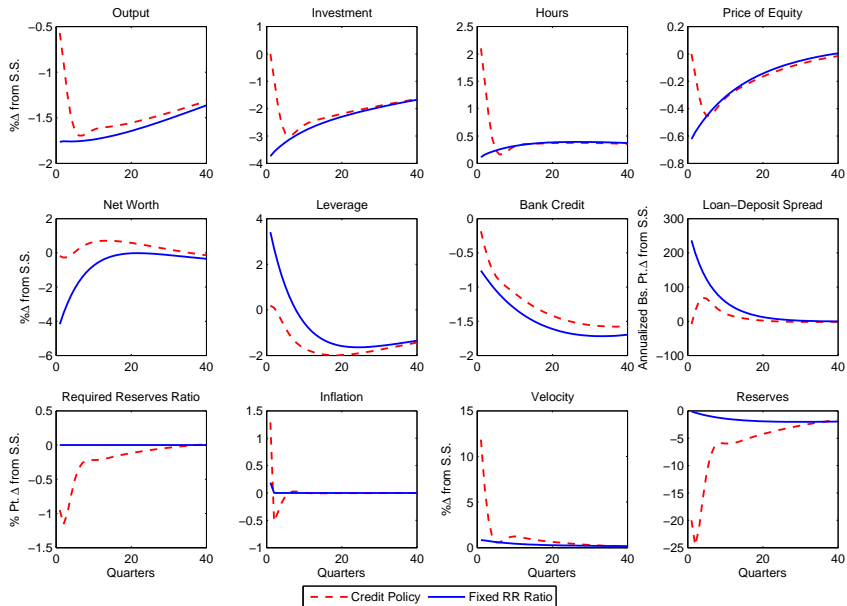
# Model Parameterization and Calibration

Description	Value	Target
<b><u>Preferences</u></b>		
Quarterly discount factor ( $\beta$ )	0.9885	Annualized real deposit rate (4.73%)
Relative risk aversion ( $\gamma$ )	2	Angeloni and Faia (2009)
Inverse of the Frisch elasticity ( $\nu$ )	3	Glocker and Towbin (2012)
Relative utility weight of leisure ( $\psi$ )	46.16	Hours worked (0.33)
<b><u>Production Technology</u></b>		
Share of capital in output ( $\alpha$ )	0.4	Labor share of output (0.64)
Capital adjustment cost parameter ( $\varphi$ )	6.76	Elasticity of price of capital w.r.t. investment-capital ratio of 0.25
Depreciation rate of capital ( $\delta$ )	0.037	Average annual ratio of investment to capital (14.8%)
<b><u>Government</u></b>		
Steady-state value of RRR ( $\bar{r}$ )	0.05	Pre-macroprudential policy period
Adjustment parameter in the RRR rule ( $\phi$ )	3.28	Standard deviation of RRR for 2010:Q4-2012:Q2 (2.33%)
Growth rate of monetary base ( $\mu$ )	0.0446	Time series average for 2006:Q1-2011:Q4
<b><u>Financial Intermediaries</u></b>		
Fraction of diverted loans ( $\lambda$ )	0.514	Annual commercial & industrial loan spread (1.96%)
Prop. transfer to the entering bankers ( $\epsilon$ )	0.0005	1.33% of aggregate net worth
Survival probability of the bankers ( $\theta$ )	0.9625	Capital adequacy ratio of 16% for commercial banks
<b><u>Shock Processes</u></b>		
Persistence of TFP process ( $\rho_z$ )	0.9821	Estimated persistence from detrended $\log TFP_t = \rho_z \log TFP_{t-1} + \epsilon_{zt}$
Std. deviation of productivity shocks ( $\sigma_z$ )	0.0183	Estimated standard deviation from detrended $\log TFP_t = \rho_z \log TFP_{t-1} + \epsilon_{zt}$
Std. deviation of financial shocks ( $\sigma_\omega$ )	0.0531	Relative volatility of bank capital w.r.t. output for 2003:Q1-2011:Q4 (1.24)

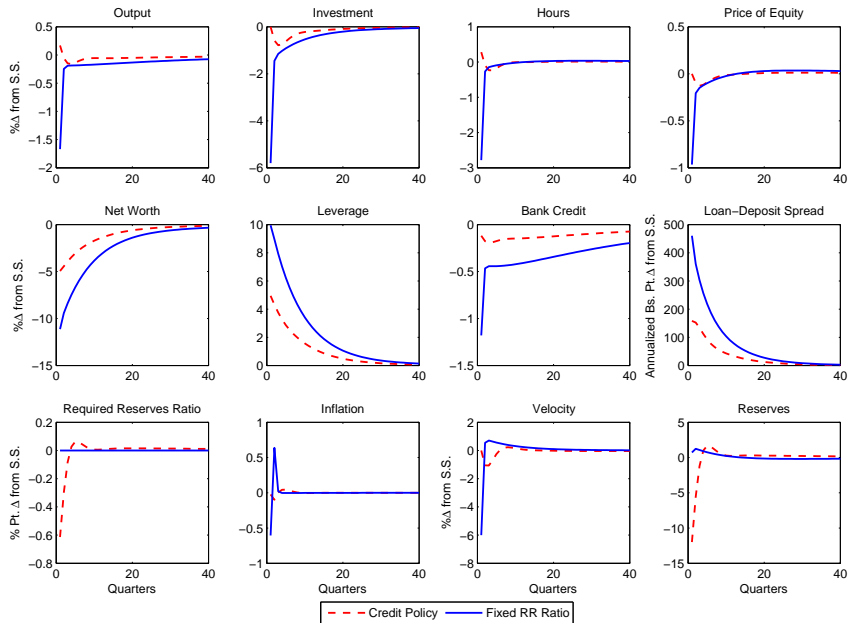
# Contribution of Financial Shocks to Business Cycles

Variable	TFP Shocks	Financial Shocks
<b>Real Variables</b>		
Output	78.32	21.68
Consumption	94.38	5.62
Investment	53.13	46.87
Hours	1.11	98.89
<b>Financial Variables</b>		
Credit	56.20	43.80
Deposits	22.80	77.20
Net worth	18.19	81.81
Leverage	15.89	84.11
Credit spread	32.47	67.53
Asset prices	52.84	47.16
<b>Monetary Variables</b>		
Inflation	3.92	96.08

# Adverse TFP Shocks



# Adverse Financial Shocks



# Impact of Credit Policy on Volatilities and Procyclicality

	Fixed Reserves	Moderate	Benchmark	Aggressive
	$\phi = 0$	$\phi = 1.45$	$\phi = 3.28$	$\phi = 4.79$
Variable	$\sigma_{rr} = 0$	$\sigma_{rr} = 1.17\%$	$\sigma_{rr} = 2.33\%$	$\sigma_{rr} = 3.50\%$
<u>Volatilities</u>				
<b>Real Variables</b>				
Output	2.51	1.92	1.70	1.60
Consumption	1.38	1.36	1.27	1.23
Investment	6.15	3.83	3.36	3.14
Hours	2.13	2.23	2.32	2.38
<b>Financial Variables</b>				
Credit	1.81	1.15	1.03	0.97
Deposits	1.88	1.36	1.65	1.94
Net worth	17.19	6.91	6.96	6.98
Leverage	15.71	6.56	6.67	6.73
Credit spread	0.58	0.29	0.27	0.26
Asset prices	1.56	0.97	0.85	0.79
<b>Monetary Variables</b>				
Inflation	0.20	0.24	0.30	0.35
<u>Cyclicality of Financial System</u>				
$\rho(\Delta_{spread}, \Delta_{GDP})^c$	-0.86	-0.08	-0.02	0.04
$\rho(\Delta_{credit}, \Delta_{GDP})^c$	0.96	0.67	0.79	0.80



# Impact of Alternative Policy Rules on Volatilities and Procyclicality

	No Reserves	Fixed Reserves	Credit Policy	Output Policy	Asset Prices Policy
	$\bar{r} = 0$	$\bar{r} = 0.05$	$\bar{r} = 0.05$	$\bar{r} = 0.05$	$\bar{r} = 0.05$
Variable	$\phi = 0$	$\phi = 0$	$\phi = 3.28$	$\phi = 1.84$	$\phi = 4.98$
<u>Volatilities</u>					
<b>Real Variables</b>					
Output	2.65	2.51	1.70	1.93	1.64
Consumption	1.39	1.38	1.27	1.28	1.22
Investment	6.66	6.15	3.36	4.63	3.28
Hours	2.58	2.13	2.32	3.42	2.42
<b>Financial Variables</b>					
Credit	1.95	1.81	1.03	1.36	1.02
Deposits	1.99	1.88	1.65	1.93	1.70
Net worth	18.39	17.19	6.96	8.26	7.03
Leverage	16.78	15.71	6.67	7.71	6.75
Credit spread	0.68	0.58	0.27	0.33	0.27
Asset prices	1.69	1.56	0.85	1.17	0.83
<b>Monetary Variables</b>					
Inflation	0.23	0.20	0.30	0.39	0.32
<u>Cyclicality of Financial System</u>					
$\rho(\Delta_{spread}, \Delta_{GDP})$	-0.85	-0.86	-0.02	-0.39	0.03
$\rho(\Delta_{credit}, \Delta_{GDP})$	0.97	0.96	0.79	0.83	0.70

# More Severe Financial Frictions

	Fixed Reserves	Credit Policy	Fixed Reserves	Credit Policy
	$\lambda = 0.25$	$\lambda = 0.25$	$\lambda = 0.75$	$\lambda = 0.75$
	$(\bar{r}_k = 12.85)$		$(\bar{r}_k = 4.28)$	
Variable	$(\overline{R_k - R} = 27 \text{ bs. pt.})$	$\phi = 3.73$	$(\overline{R_k - R} = 67 \text{ bs. pt.})$	$\phi = 2.82$

## Volatilities

### Real Variables

Output	2.25	1.61	2.79	1.81
Consumption	1.37	1.29	1.43	1.28
Investment	4.78	2.87	7.39	3.86
Hours	1.11	2.28	2.96	2.37

### Financial Variables

Credit	1.42	0.88	2.15	1.17
Deposits	1.04	1.50	2.90	1.97
Net worth	20.91	6.49	15.90	7.19
Leverage	19.78	6.46	14.18	6.73
Credit spread	1.06	0.36	0.42	0.23
Asset prices	1.21	0.72	1.87	0.97

### Monetary Variables

Inflation	0.11	0.32	0.28	0.29
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## Cyclicalities of Financial System

$\rho(\Delta_{spread}, \Delta_{GDP})$	-0.88	-0.02	-0.86	-0.01
$\rho(\Delta_{credit}, \Delta_{GDP})$	0.96	0.86	0.97	0.68

# More Volatile Asset Prices

	Fixed Reserves	Credit Policy	Fixed Reserves	Credit Policy
	$\varphi = 0.5$ ( $\bar{\kappa} = 6.25$ )	$\varphi = 0.5$	$\varphi = 13.75$ ( $\bar{\kappa} = 6.25$ )	$\varphi = 13.75$
Variable	$(\overline{R_k} - R = 48 \text{ bs. pt.})$	$\phi = 4.13$	$(\overline{R_k} - R = 48 \text{ bs. pt.})$	$\phi = 2.7$

## Volatilities

### Real Variables

Output	2.64	2.08	2.42	1.60
Consumption	1.16	1.12	1.58	1.40
Investment	7.43	5.36	5.20	2.52
Hours	2.28	2.19	2.03	2.35

### Financial Variables

Credit	0.84	0.69	2.79	1.36
Deposits	1.37	1.29	2.25	1.86
Net worth	8.34	6.63	24.16	7.13
Leverage	7.94	6.54	21.72	6.68
Credit spread	0.31	0.30	0.78	0.27
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### Monetary Variables

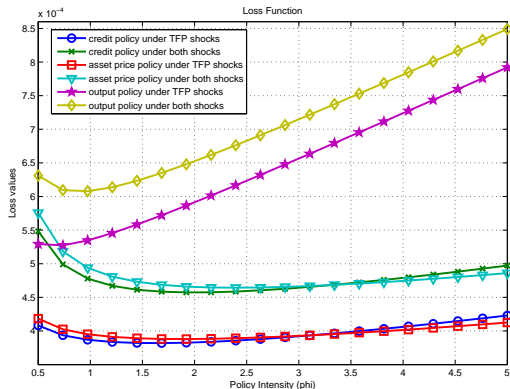
Inflation	0.22	0.25	0.19	0.31
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## Cyclicalities of Financial System

$\rho(\Delta_{spread}, \Delta_{GDP})$	-0.85	0.03	-0.87	0.03
$\rho(\Delta_{credit}, \Delta_{GDP})$	0.61	0.46	0.97	0.81

# Welfare Evaluation: Loss Function Approach

	Fixed Reserves Policy	Credit Policy	Output Policy	Asset Prices Policy
	$\bar{r} = 0.05$	$\bar{r} = 0.05$	$\bar{r} = 0.05$	$\bar{r} = 0.05$
Loss values	$\phi = 0$	$\phi = 3.28$	$\phi = 1.84$	$\phi = 4.98$
Under only TFP shocks	4.3613e-04	3.9560e-04	5.8147e-04	4.1233e-04
Under both shocks	6.4556e-04	4.6789e-04	4.8579e-04	6.4341e-04



# Conclusion

- ▶ RRR policies that are meant to stabilize credit growth work as a macro-prudential tool under the existence of TFP and financial shocks.
- ▶ However, reduced volatilities of real and financial variables come at the expense of higher inflation volatility.
- ▶ For further work, small open economy features and optimal monetary policy considerations shall be introduced in order to reconcile the analysis more with the experience of emerging economies.

**THANK YOU**

# Workers

$$\max_{c_t, l_t, b_{t+1}, M_{t+1}} E_0 \sum_{t=0}^{\infty} \beta^t u(c_t, l_t)$$

$$\text{s.t.} \quad c_t + b_{t+1} + \frac{M_{t+1}}{P_t} = w_t(1 - l_t) + R_t b_t + \frac{M_t}{P_t} + \frac{\Pi_t}{P_t} + \frac{T_t}{P_t}$$

$$\text{and} \quad c_t \leq \frac{M_t}{P_t} + \frac{T_t}{P_t} + R_t b_t - b_{t+1}$$

$$\Rightarrow \quad u_c(t) = \beta E_t \left\{ R_{t+1} u_c(t+1) \right\}$$

$$\frac{u_l(t)}{P_t w_t} = \beta E_t \left\{ \frac{u_c(t+1)}{P_{t+1}} \right\}$$

# Bankers

- ▶ Banker  $j$  collects deposits from worker  $i \neq j$ , lend to a large number of identical firms, and hold required “reserves”

$$q_t s_{jt} = (1 - rr_t) b_{jt+1} + n_{jt}$$

- ▶
- ▶ Net worth accumulation into the next period,

$$\begin{aligned} n_{jt+1} &= R_{kt+1} q_t s_{jt} - R_{t+1} b_{jt+1} + rr_t b_{jt+1} \Rightarrow \\ n_{jt+1} &= \left[ R_{kt+1} - \left( \frac{R_{t+1} - rr_t}{1 - rr_t} \right) \right] q_t s_{jt} + \left( \frac{R_{t+1} - rr_t}{1 - rr_t} \right) n_{jt} \\ &\quad \text{ESP}_{t+1} \qquad \qquad \qquad \text{RR}_{t+1} \end{aligned}$$

- ▶ Required reserves make net worth financing more preferable

$$\frac{d\text{ESP}_{t+1}}{drr_t} < 0 \quad \text{and} \quad \frac{d\text{RR}_{t+1}}{drr_t} > 0$$

- ▶ Banks operate only if  $E_t \{ \beta^{1+i} \Lambda_{t,t+1+i} \text{ESP}_{t+1+i} \} \geq 0 \forall i$



## Bankers cont'd

- ▶ Bankers maximize the terminal value of their net worth

$$V_{jt} = \max_{s_{jt}} E_t \sum_{i=0}^{\infty} (1 - \theta) \theta^i \beta^{1+i} \Lambda_{t,t+1+i} n_{jt+1+i}$$

- ▶ s.t. an agency problem: After borrowing from households, bankers can divert  $\lambda$  fraction of their total assets.
- ▶ Incentive compatibility:

$$V_{jt} \geq \lambda q_t s_{jt}$$

# Bankers cont'd



## Bankers cont'd

$V_{jt}$  can be written as follows:

$$V_{jt} = \nu_t q_t s_{jt} + \eta_t n_{jt}$$

where

$$\nu_t = E_t \left\{ (1 - \theta) \beta \Lambda_{t,t+1} ESP_{t+1} + \beta \Lambda_{t,t+1} \theta xx_{t,t+1} \nu_{t+1} \right\}$$

$$\eta_t = E_t \left\{ (1 - \theta) \beta \Lambda_{t,t+1} RR_{t+1} + \beta \Lambda_{t,t+1} \theta zz_{t,t+1} \eta_{t+1} \right\}$$

with  $xx_{t,t+1} = q_{t+1} s_{jt+1} / q_t s_{jt}$  and  $zz_{t,t+1} = n_{jt+1} / n_{jt} \quad \forall j$

## Bankers cont'd

- ▶  $V_{jt}$  can be written as follows:

$$V_{jt} = \nu_t q_t s_{jt} + \eta_t n_{jt} \geq \lambda q_t s_{jt}$$

- ▶ When it binds:

$$q_t s_{jt} = \frac{\eta_t}{\lambda - \nu_t} n_{jt} = \kappa_t n_{jt}$$

- ▶ Financial intermediaries may fund non-financial firms only up to an “endogenous multiple” of their net worth
- ▶ We aggregate over  $j$  and get:  $q_t s_t = \kappa_t n_t$

# Net Worth Evolution

- ▶  $n_{t+1} = n_{et+1} + n_{nt+1}$

- ▶  $\theta \rightarrow$  survival probability of bankers.

$$n_{et+1} = \theta \left[ ESP_{t+1} \kappa_t + RR_{t+1} \right] n_t$$

- ▶  $\frac{\epsilon}{(1-\theta)}$   $\rightarrow$  fraction of exiting bankers' net worth that is transferred to new entrants as start-up funds

- ▶  $\Rightarrow n_{nt+1} = (1 - \theta) \frac{\epsilon}{(1-\theta)} n_t = \epsilon n_t$

- ▶ Law of Motion for Aggregate Net Worth

$$n_{t+1} = \left\{ \theta \left[ ESP_{t+1} \kappa_t + RR_{t+1} \right] + \epsilon \right\} n_t$$

# Firms

- ▶ Finance capital acquisition each period via issuing equity claims which are purchased by financial intermediaries

$$q_t s_t = q_t K_{t+1}$$

- ▶ Produce with a CRS technology by using capital and labor

$$\exp(z_t) F(K_t, H_t)$$

- ▶ Labor demand satisfies

$$w_t = \exp(z_t) F_H(K_t, H_t)$$

- ▶ Zero profit condition leads to following condition of return on capital:

$$R_{kt} = \frac{\exp(z_t) F_K(K_t, H_t) + q_t(1 - \delta)}{q_{t-1}}$$

# Competitive Equilibrium

- ▶ Nominal monetary base and prices grow constantly in this model, which renders the equations listed above non-stationary. Therefore, following Cooley and Hansen (1989), we make the model stationary by applying the following normalizations:  $\widehat{P}_t = P_t/M_{0t+1}$  and  $\widehat{m}_t = M_{t+1}/(\widehat{P}_t M_{0t+1})$  and solve the model locally around a deterministic steady state.
- ▶ A competitive equilibrium of this model economy is defined by sequences of allocations  $\{c_t, k_{t+1}, i_t, l_t, h_t, s_t, n_t, n_{et}, n_{nt}, b_{t+1}, \Lambda_{t,t+1}, \nu_t, \eta_t, \kappa_t, \rho_{t,t+1}, \chi_{t,t+1}, \widehat{m}_{t+1}, \pi_t\}_{t=0}^{\infty}$ , prices  $\{q_t, R_{kt+1}, R_{t+1}, w_t, \widehat{P}_t\}_{t=0}^{\infty}$ , shock processes  $\{z_t, \mu_t\}_{t=0}^{\infty}$  and the government policy  $\{rr_t\}_{t=0}^{\infty}$  such that
  - (i) allocations solve household's, financial intermediary's, firm's, and capital producer's problems at the equilibrium prices.
  - (ii) markets for factor inputs clear.
  - (iii) aggregate resource constraint is satisfied.